

Slope-Point Form - Equation of a Line

(day 1)

The ^{3rd} way to write an equation of a line:

$$y - y_1 = m(x - x_1)$$

$m = \text{slope}$

x and $y = \text{variables}$

x_1, y_1 } Represent a point (x_1, y_1)
They will be replaced with numbers.

For example:

$$y - 5 = \frac{3}{4}(x - 1)$$

slope = $\frac{3}{4}$

Passes thru point $(1, 5)$

$$y + 6 = -2(x - 7)$$

slope = -2

$$y - (-6) = -2(x - 7)$$

passes thru point $(7, -6)$

Ex. write the equation of a line that:

a) passes thru $(x_1, y_1) = (6, -5)$

$$\text{slope} = \frac{1}{2}m$$

$$y - y_1 = m(x - x_1)$$

$$y - -5 = \frac{1}{2}(x - 6)$$

$$y + 5 = \frac{1}{2}(x - 6)$$

b) passes thru $(x_1, y_1) = (-4, 7)$

$$\text{slope} = \frac{4}{3}m$$

$$y - y_1 = m(x - x_1)$$

$$y - 7 = \frac{4}{3}(x - -4)$$

$$y - 7 = \frac{4}{3}(x + 4)$$

Ex. write the equation (in all 3 formats) for a line that passes thru $(-1, -5)$ and has a slope of 3.

line that passes through $(-1, -5)$ and has a slope of 3.

$$y = mx + b$$

① $y - y_1 = m(x - x_1)$

$$y - -5 = 3(x - -1)$$

slope point form

$$y + 5 = 3(x + 1)$$

$$Ax + By + C = 0$$

② $y + 5 = 3(x + 1)$

$$y + 5 = 3x + 3$$

$$y = 3x - 2$$

slope-intercept form

③ $y = 3x - 2$

$$(-3x + y + 2 = 0) \cdot (-1)$$

$$3x - y - 2 = 0$$

general form

Practice on whiteboards

Slope Point Form (day 2)

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⊗ If we only know 2 points on a line, we can write the equation using slope point form:

- ① Label the points with x_1, y_1, x_2, y_2
- ② Calculate the slope
- ③ substitute the slope and one of the points into the slope-point form equation.

Ex. write the equation of the line that passes thru $(-6, -3)$ and $(4, 5)$ in all 3 ways.
 x_1, y_1 x_2, y_2 * only 2 points!

① Find slope:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{5 - (-3)}{4 - (-6)}$$

$$= \frac{5 + 3}{4 + 6}$$

$$= \frac{8}{10}$$

$$m = \frac{4}{5}$$

② slope-point form:

$$y - y_1 = m(x - x_1)$$

$$y - (-3) = \frac{4}{5}(x - (-6))$$

$$y + 3 = \frac{4}{5}(x + 6)$$

③ Slope Intercept form:

$$y + 3 = \frac{4}{5}(x + 6)$$

$$y + 3 = \frac{4}{5}x + \frac{24}{5}$$

$$-3$$

$$y = \frac{4}{5}x + \frac{9}{5}$$

$$\frac{4}{5} \times \frac{6}{1} = \frac{24}{5}$$

$$\frac{24}{5} - \frac{3}{1} = \frac{24}{5} - \frac{15}{5} = \frac{9}{5}$$

* keep as fractions *

④ General Form:

$$y = \frac{4}{5}x + \frac{9}{5}$$

$$-\frac{4}{5}x - \frac{9}{5} \quad -\frac{4}{5}x - \frac{9}{5}$$

$$\left(-\frac{4}{5}x + y - \frac{9}{5} = 0\right) \cdot (-1)$$

$$\left(\frac{4}{5}x - y + \frac{9}{5} = 0\right) \cdot (5)$$

$$4x - 5y + 9 = 0$$

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